



# The Bright Side of Mathematics

## Start Learning Logic - Part 3

Logical operations:

**Conditional:** For two logical statements  $A, B$ ,  
 $A \rightarrow B$  denotes the conditional.

Truth table

A	B	$A \rightarrow B$
T	T	T
T	F	F
F	T	T
F	F	T

$\Rightarrow$  means  $\rightarrow$  gives tautology

A	B	$A \wedge B$	$A \wedge B \rightarrow B$
T	T	T	T
T	F	F	T
F	T	F	T
F	F	F	T

We can write:

$$A \wedge B \Rightarrow B$$

**Biconditional:** For two logical statements  $A, B$ ,  
 $A \leftrightarrow B$  denotes the biconditional.

Truth table

A	B	$A \leftrightarrow B$
T	T	T
T	F	F
F	T	F
F	F	T

$\Leftrightarrow$  means  $\leftrightarrow$  gives tautology

Example: (a)  $A \leftrightarrow B \Leftrightarrow (A \rightarrow B) \wedge (B \rightarrow A)$

(b)  $A \rightarrow B \Leftrightarrow \neg B \rightarrow \neg A$  (contraposition)

If there is fog, then we have poor visibility

If we don't have poor visibility, there is no fog.

Deduction rules: (how to get new true propositions from other true propositions)

Modus ponens: If  $A \rightarrow B$  true and  $A$  true, then:  $B$  true

A	B	$A \rightarrow B$
T	T	T
T	F	F
F	T	T
F	F	T

Chain syllogism: If  $A \rightarrow B$  true and  $B \rightarrow C$  true, then:  $A \rightarrow C$  true

Reductio ad absurdum: If  $A \rightarrow B$  true and  $A \rightarrow \neg B$  true, then:  $\neg A$  true